# The membrane potential

it vary rapidly over large distances

controls a vast number of nonlinear gates – ionic channels – that provide a very rich substrate for implementing nonlinear operations.

channels transduce stimuli into changes of the membrane potential and such voltage changes back into the release of neurotransmitter or the contraction of muscles.



Nerve and muscle are *excitable tissues* - they have the ability to generate and propagate electrical signals. Membrane potential is influenced by:

- Concentration gradients
- Permeability of the membrane to ions

$$\Delta \Psi = \frac{RT}{F} \ln \frac{P_{K}[K_{out}^{+}] + P_{Na}[Na_{out}^{+}] + P_{Cl}[Cl_{in}^{-}]}{P_{K}[K_{in}^{+}] + P_{Na}[Na_{in}^{+}] + P_{Cl}[Cl_{out}^{-}]}$$



Single-channel currents



#### Ion channel

ion-permeation pathway through the membrane

#### Selectivity filter

(narrowest constriction in the 'open' conformation)

# *Elements that control the gate*

(ligand-binding sites, voltage-sensor, pH-sensor, temperaturesensor, mechanicaldeformation sensor)



(narrowest constriction in the 'closed' conformation)

#### **Depending on the type of the channel, this gating process may be driven by:**





#### Membrane can be

- Depolarized
- Hyperpolarized
- Repolarized





#### At rest:

Membrane potential is mostly due to  $K^+$ Membrane is almost impermeable to  $Na^+$ 

#### When ion channels open:

*Ions move in or out depending on electro-chemical gradient. Resulting influx changes membrane potential.* 



#### An action potential

# a transient depolarization from the resting membrane potential.

- *All-or-none response*
- Refractory period
- Moves at a constant speed
- The peak potential is independent on distance

Pulses are quantized all the same

- pulse length 1 ms
- **u** pulse strength  $\Delta V = 100 \text{ mV}$

length and strength are determined by kinetics of ion channels



Time (msec)

#### **Global Transitions Induced by Voltage:**



## **Action Potential – Na and K Currents:**



#### **Action Potential – Channel Conductance:** nS ? Na<sup>+</sup> channel G<sub>K</sub> 160 120 ? K<sup>+</sup> channel $G_{Na}$ 40 Na+ Leakage channel K<sup>+</sup>out **K**+ -80 40 mV 0 -40 Ψ1 Ψ2

#### **Action Potential – Channel Conductance:**





- Very little Na<sup>+</sup> will cause a large depolarization.
- [Na]: and [Na]o don't change significantly.

• It responds to a small depolarization (from -70 to -50mV). This increases  $P_{Na}$  500- 5000 fold



Sodium channels





**Cross section** 





Inactivated

#### Voltage Gated Sodium Channel



Voltage-gated Ion Channels: Function helix 4: voltage-sensitive, rotating, sliding



Voltage-dependent gating





#### Voltage-gated Na<sup>+</sup> channels requires two gates

Activation gate:

Closed at resting membrane potential Opens when cell depolarizes, allowing Na<sup>+</sup> to enter

Inactivation gate:

Open at resting membrane potential Closes when cell depolarizes, but has 0.5 ms delay

Both reset when cell repolarizes

During repolarization caused by K<sup>+</sup> leaving the cell, the two gates reset to their original positions.



### **Action Potential – Channel Conductance:**



# K<sup>+</sup> channel

• highly selective (permeability for  $K^+$  is at least 10,000 times higher than for Na  $^+$ )

- opens slowly
- ion conductance is highly efficient s1 S2 S3 S4 S5
   limit, 10<sup>8</sup> ions/sec)
  - has voltage-sensor
  - *inactivates rapidly*







# Ion movements during the action potential



# **Graded Potentials**



Graded potentials (depolarization or hyperpolarizations)

- Location any receptor on dendrites and cell body
- Begin at point where ions enter ECF (local current flow)
- Local current net movement of positive charges
- Strength (= amplitude) ~ strength of triggering event
- Amplitude varies inversely with distance
- They travel until they reach the trigger zone
- They can be summed to reach threshold







# Stimuli stronger than the threshold result in an *action potential*.



does not initiate an action potential. Stimulus Stimulus Synaptic terminal -40 -70 mV Stimulus Time Cell body -40 -55 -70 mV Trigger Trigger Time zone zone -40 -55 Axon -70 mV Time Graded potential No action Action below threshold potential

(a) A graded potential starts above threshold (T) at its initiation

point, but decreases in strength as it travels through the cell

body. At the trigger zone it is below threshold and therefore

(b) A stronger stimulus at the same point on the cell body creates a graded potential that is still above threshold by the time it reaches the trigger zone, so an action potential results.



Subthreshold potential vs. suprathreshold potential

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#### Dendrite (cut) **Integration of Neural Information Transfer** Synaptic knobs Multiple graded potentials are integrated at axon odendria hillock to evaluate necessity of AP Dendrite (c Glial cell **1.** Spatial Summation: stimuli from different lxon processes Myelin sheath locations are added up Presynaptic axon terminal Dendrite (b) In a convergent pathway, many }Trigger presynaptic neurons converge to }Trigger Action potential zone influence a smaller number of postsynaptic neurons. action potential 2. Temporal Summation: sequential stimuli added up Threshold X2 Time (msec) Threshold Membrane Stimulus (X) X<sub>1</sub> X<sub>2</sub> Time (msec)

# The Generation of an Action Potential



#### Trigger Zone

- Usually Axon Hillock
- and/or Initial segment of axon
- Many Na<sup>+</sup> Channels

#### Some stimuli may be inhibitory

• Hyperpolarizing effect



Signal transmition along the neuron.

#### Negative Feedback Cycle Underlies Falling Phase of the Action Potential



## Absolute & Relative Refractory Periods



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# Equivalent Circuit of the Membrane Connected to the Voltage Clamp



#### Propagation of action potentials in unmyelinated axons.





# Conduction speed depends

#### **1.** Axon diameter (the larger the faster)

- Size constraints on axons become problem with increasing organismal complexity

#### 2. Membrane resistance

(a)

- High resistance of myelin sheath reduces leakage of current (ion) flow between axon and ECF

#### - Saltatory Conduction from node to node

O

One giant axon from a squid



400 myelinated mammalian axons

would require a nerve this size if each mammalian axon were the size of a squid giant axon







# Among all types of neurons, myelinated neurons conduct action potentials most rapidly.



In nerve fibres with diameter  $\geq 1 \ \mu m$  a myelin sheath are broken at intervals of  $\approx 1-1.5 \ mm$ .

Action potential propagation in myelinated axons

Nodes of Ranvier

Membrane resistance lowest at these points

- **AP** Propagation
  - Starts at trigger zone
  - AP flows to 1st Node of Ranvier
  - Node has high density of voltage gated Na<sup>+</sup> channels
  - Na<sup>+</sup> re-entry boosts strength of AP





### **The Membrane Electrical Analog:**





## **The Axon Electrical Analog:**



I<sub>i</sub> (x) – axial current

 $I_m(x)$  – ion current through membrane

R<sub>i</sub> – axoplasm resistance

**R**<sub>m</sub> – membrane resistance

- **C**<sub>m</sub> membrane capacitance
- **V**<sub>m</sub> membrane potential
- a diameter of axon
- dx unit length

 $\kappa$  – electrical conductivity of axoplasm

#### **The Axon Electrical Analog:**



#### **The Axon Electrical Analog:**



$$\frac{\partial V'_m(x,t)}{\partial t} = \frac{I_c}{C_m}$$

$$I_{total} = C_m \frac{\partial V'_m}{\partial t} + I_{ionic}$$

#### V'<sub>m</sub> – difference in membrane potential from resting state

#### **Passively Spreading Potential:**



Change in the axial current must be balanced by the current through the membrane

$$I_{x}(x) - I_{x}(x + dx) = \frac{\partial I_{x}}{\partial x} dx = 2\pi a \left( j_{q,r}(x) + C \frac{\partial V_{m}}{\partial t} \right) dx$$
All ionic currents
Charge piling on the capacitor
$$Unknown functions: \begin{bmatrix} V_{m}(x,t) \\ I_{i}(x,t) \\ i = (x, t) \end{bmatrix}$$

 $J_{q,r}(x, t)$ 

### **Linear Cable Equation:**

Space constant:

$$\lambda_{axon} = \sqrt{\frac{a\kappa}{2G_{total}}}$$
$$\tau \approx \frac{C}{1}$$

Time constant:

$$\cong \frac{C}{G_{total}}$$

#### Linear cable equation:

$$(\lambda_{axon})^2 \frac{\partial^2 V'_m}{\partial x^2} - \tau \frac{\partial V'_m}{\partial t} = V'_m$$

Solution:

$$V(x,t) = const \cdot \exp\left(\frac{-t}{\tau}\right) * t^{-1/2} \exp\left(\frac{-x^2}{4t(\lambda_{axon})^2 \tau}\right)$$

### **Characteristic parameters of nerve "cables" :**

	Frog muscle neuron		Squid gigantic axon	
	a = 75 μm		$a = 600 \ \mu m$	
	External	Internal	External	Internal
Na <sup>+</sup>	120 mM	9.2 mM	460 mM	50 mM
K+	2.5 mM	140 mM	10 mM	400 mM
Cl-	120 mM	3-4 mM	540 mM	40-100 mM
Resting potential:	-90 mV		-60 mV	
Space constant $(\lambda_{axon})$	<b>2 mm</b>		<b>5 mm</b>	
Time constant $(\tau)$	24 ms		0.7 ms	
R <sub>m</sub>	4000 Ohm/cm <sup>2</sup>		700 Ohm/cm <sup>2</sup>	
R <sub>i</sub>	200 Ohm/cm		30 Ohm/cm	
C <sub>m</sub>	6 μF/cm <sup>2</sup>		6 μF/cm <sup>2</sup>	

## **Non-Linear Cable Equation:**

- 1. The wave propagation requires threshold stimulus
- 2. If the stimulus is too low or is of a wrong sign, it will result in decaying response (as described by the linear cable equation)
- 3. Above threshold stimulus creates a traveling wave of excitation, so that the response at a distance from the point of stimulation does not depend on the magnitude of the stimulus and has a predicted shape
- 4. The traveling wave moves at a constant speed along the axon.

# Voltage-gating hypothesis:



$$V(x,t) = V\left[0, \left(t - \frac{x}{\upsilon}\right)\right]$$

#### **NON-Linear Cable Equation:**

$$(\lambda_{axon})^2 \frac{\partial^2 V'_m}{\partial x^2} - \tau \frac{\partial V'_m}{\partial t} = V'_m$$

 $\sqrt{2} d^2 U$ 

2

Linear cable equation:



$$(\lambda_{axon})^2 \frac{\partial^2 V'_m}{\partial x^2} - \tau \frac{\partial V'_m}{\partial t} = V'_m \frac{(V'_m - V_1)(V'_m - V_2)}{V_1 V_2}$$

NON-Linear cable equation:

$$\frac{\lambda_{axon}}{\upsilon}\right)^2 \frac{d^2 V'_m}{dt^2} - \tau \frac{\partial V'_m}{\partial t} = V'_m \frac{(V'_m - V_1)(V'_m - V_2)}{V_1 V_2}$$

$$\upsilon = \pm \frac{\lambda_{axon}}{\tau} \sqrt{\frac{2}{s}} \left(\frac{s}{2} - 1\right)$$
$$s = \frac{V_1}{V_2}$$

Traveling-wave solution



# Signal transmition between neurons.



# Synaptic transmission

There are:

#### *electric synapses (excitatory only) chemical synapses (excitatory, inhibitory or facilitating)*

**Synaptic cleft** – the space separating membranes of the two cells making the connection (26 - 40 nm).



# There are about 10<sup>15</sup> synapses in a human brain.





The Ca-concentration and the pH level controls the function of an electric synapse

A fish has many electric synapses, these fast working units make possible the lightning – fast whisk of their tail. A good lot of electric synapses may be found in some parts of the human brain, too, (hippocampus, hypothalamus, spinal marrow, etc.), as well as in the retina.



# Synapse: most vulnerable step in signal propagation

Many disorders of synaptic transmission, *e.g.*:

- Myasthenia gravis (PNS)
- Parkinson's (CNS)
- Schizophrenia (CNS)
- *Depression* (CNS)
- Many toxins

Axon terminals have mitochondria & synaptic vesicles containing neurotransmitter





#### Synaptic transmission

1. Action potential, moving along axon's voltage-gated Na <sup>+</sup> and K<sup>+</sup> channels, arrives at terminal.

**2.** Action potential opens voltage-gated Ca<sup>++</sup> channels.

3. Ca<sup>++</sup> influx triggers neurotransmitter release into the synaptic cleft.

4. The binding of neurotransmitters to receptor proteins in the postsynaptic membrane is linked to an alteration in its ion permeability.





Trasmission of the nervous impulse

The transmitter release of about 10 vesicles is required to generate a postynaptic potential that is big enough to result in an action potential.

#### *Ligand-gated channel* – acetyl choline gated channel



# Transmitter effects on $E_m$



- Most chemical stimuli result in an influx of cations
   This causes a depolarization of the membrane potential
- At least one transmitter opens an anion influx
  - This results in a hyperpolarization.

*Cation-conducting channels* - acetylcholine-, serotonin- and glutamate receptors

*Anion-conducting channels* - glycine and gaminobutiric (GABA) acid -gated receptors

# **EPSPs** and **IPSPs**

- If the transmitter opens a cation influx, the resulting depolarization is called an *Excitatory Post Synaptic Potential* (EPSP).
- These individual potentials are sub-threshold.
- If the transmitter opens an anion influx, the resulting hyperpolarization is called an *Inhibitory Post Synaptic Potential* (IPSP)
- All these potentials are additive.

#### Excitatory synapses







Excitatory amino acid neurotransmitters

#### Inhibitory synapse



Inhibitory amino acid neurotransmitters

# Neurotransmitters and receptors in the autonomic

#### nervous system



#### Neurotransmitters:

- Acetylcholine; a class by itself
- Amino acids; Glycine, Glutamate, Gamma-aminobutyric acid (GABA), Aspartate
- Amino acid-derived amines; Catecholamines (Dopamine, Norepinephrine, Epinephrine), Serotonin (5-HT), Histamine
- Purines; Adenosine, ATP
- Polypeptides; Enkaphalins, Endorphins, Dynorphins, Substance P, Somatostatin, Bradykinin, Neuropeptide Y







#### Signal integration



(a) Temporal summation



(b) Spatial summation

# **Postsynaptic Responses**

#### Can lead to either EPSP or IPSP

Any one synapse can only be either excitatory or inhibitory



Slow response, direct coupling

Slow synaptic potentials

Involve G-proteins and 2<sup>nd</sup> messengers Can open <u>or</u> close channels or change protein composition of neuron

#### Fast synaptic potentials

Opening of chemically gated ion channel Rapid & of short duration



# **Post-synaptic** integration

inhibition



#### **Presynaptic facillitation and inhibition**



### Factors Influencing Transmitter Release

- Amplitude of arriving Action Potential
- Nerve terminal's ability to synthetize, package, store, mobilize, and release neurotransmitter
- Prior activity of presynaptic ending
- Concentration of Ca<sup>++</sup> in ECF

# Factors that limit the maximum response of a receptor cell to strong stimuli

- A finite number of channels
- Receptor potential cannot exceed the reversal potential of the receptor current
- Impulse frequencies are limited by the refractoriness



In <u>normal brain activity</u>, neurotransmitters are constantly being released, re-absorbed, and then broken down.

In <u>depression</u>, fewer neurotransmitters are being released which leads to a reduction in stimulation of target brain cells.



# Antidepressants

Tricyclic Agents: (ELAVIL; TOFRANIL; PAMELOR) – block the re-uptake of serotonin u serotonin NE dopamine

Heterocyclic Agents: (DESYREL; WELLBUTRIN; ZYBAN) – block different neurotransmitter to variable degrees

<u>Selective Serotonin Reuptake Inhibitors</u> (SSRI's): ( PROZAC; ZOLOFT; PAXIL; CELEXA )

Serotonin - NE Re-uptake Inhibitors (SNRI's) ( EFFEXOR )

Monoamine Oxidase Inhibitors (MAOI's): ( NARDIL PARNATE)



u serotonin, NE, dopamine

## **GABA**

**4** *GABA* binds to *GABA* receptor (coupled to a chloride channel – chloride enter the cell).



**4** The cells fire less – a greater inflow of chloride – more negative interior – promoting neuronal hyperpolarization.

### Alcohol acts on channels

(I) Ethanol binds to the GABA receptor inhibiting it – relaxation and sedation.

(II) Alcohol opens a specific type of ionic channel (GIRK).

This channel allows that brain cells eliminate potassium, thus reducing their activity.

The result is a slow-down in brain function, perceived as a relaxing sensation by the drinker.

#### The Dopamine Function in the Brain

*A neurotransmitter responsible for motivation and pleasure.* 

**4** The dopamine molecules attach themselves to dopaminergic receptors in the membrane of the post-synaptic neuron.





**4** It blocks the reuptake of dopamine in dopaminergic synapeses at the brain reword system.

**4** Dopamine remains in the synaptic gap. The effect remains until cocaine is removed. ,, The pleasure effect "

**4** The prolonged use of cocaine makes the brain to adapt to it - the synthesis of dopamine decreases.

**4** When without cocaine the drug user experiences the opposite of pleasure (due to the low levels of dopamine) - fatigue, depression and altered moods.



# Total power used by the brain $\sim 20$ watt