Transport across the biological membrane





Maximal entropy principle:

 $dS = (\partial S/\partial E_1)dE_1 + (\partial S/\partial E_2)dE_2 = [(\partial S/\partial E_1) - (\partial S/\partial E_2)]dE_1 = 0$

where we considered: $dE_2 = - dE_1$

 $(dS/dE_{1,2}) = 1/T_{1,2}$... thermodynamic definition of temperature

$$\mathbf{T}_1 = \mathbf{T}_2$$





Maximal entropy principle:

 $dS = (\partial S/\partial V_1)dV_1 + (\partial S/\partial V_2)dV_2 = [(\partial S/\partial V_1) - (\partial S/\partial V_2)]dV_1 = 0$

where we considered: $dV_2 = - dV_1$

 $(\partial S/\partial V_{1,2})E,N = p_{1,2}/T...$ Thermodynamic identity

 $p_1 = p_2$

Particle flow



Maximal entropy principle:

 $dS = (\partial S/\partial N_1)dN_1 + (\partial S/\partial N_2)dN_2 = [(\partial S/\partial N_1) - (\partial S/\partial N_2)]dN_1 = 0$

where we considered: $dN_2 = - dN_1$

 $(\partial S/\partial N_{1,2})E, V = \mu_{1,2} / T \dots$ Thermodynamic definition of a chemical potential μ :

 $\mu_1 = \mu_2$

Membrane Transport and Human Disease

- *Cystic Fibrosis and CFTR* (the most common fatal childhood disease in Caucasian populations). Inadequate secretion of pancreatic enzymes leading to nutritional deficiencies, bacterial infections of the lung and respiratory failure, male infertility.
- **Bile Salt Transport Disorders** Several ABC transporters, specifically expressed in the liver, have a role in the secretion of components of the bile, and are responsible for several forms of progressive familial intrahepatic cholestasis, that leads to liver cirrhosis and failure.
- *Retinal Degeneration* The ABCA4 gene products transports retinol (vitamin A) derivatives from the photoreceptor outer segment disks into the cytoplasm. A loss of ABCA4 function leads to retinitis pigmentosa and to macular dystrophy with the loss of central vision.
- *Mitochondrial Iron Homeostasis* ABCB7 has been implicated in mitochondrial iron homeostasis. Two distinct missense mutations in ABCB7 are associated with the X-linked sideroblastic anemia and ataxia.
- *Multidrug Resistance* ABC genes have an important role in MDR and at least six different ABC transporters are associated with drug transport.

Nobel Prizes in Membrane Transport

1978	Peter Mitchell (UK)	Concept of chemiosmotic coupling
1988	Johan Deisenhofer (D) Robert Huber (D) Hartmut Michel (D)	Structure of electron-translocating photosynthetic reaction centre
1991	Erwin Neher (D) Bert Sakmann (D)	Patch clamp technique for single channel recording
1997	Jens-Christian Skou (DK) Paul Boyer (USA) John Walker (UK)	Mechanisms of ATP-driven ion translocation
2004	Peter Agre (USA) Rod MacKinnon (USA)	Structure of water- and ion- channels

General comment on transport process

Transport is the flux of an entity in response to a driving force:

Flux
$$j_i = \rho_i \omega_i F$$

where ρ_i is the density of the material or species i (or concentration, c_i), and ω_i is its equivalent mobility under the influence of a force.

The flux of i (j_i) is the net movement of i per unit area per unit time; the units are i cm⁻² s⁻¹.

Force can be expressed as a potential gradient: $F = -\frac{\partial U}{\partial x}$ In one dimension:

$$j_i = -v_i \frac{\partial U}{\partial x}$$
 in 3D $j_i = -v_i \nabla U$

Examples of Transport



Homeostasis



It is maintained by a combinations of fluxes

Membranes are flexible, non-extendible, selfsealing, differentially permeable barriers that separate "IN" from "OUT"



Function of transport



- Cell volume osmolarity
- Intracellular pH
- Membrane potential
- Ions gradients
- Exchange of molecules

Ion	In	Out	
Potassium	140 mM	1 – 4.5 mM	
Sodium	5 – 15 mM	145 mM	
Magnesium	5 mM	<u>1 – 2 mM</u>	
Calcium >	<mark>0.5</mark> μΜ	2.5 - 5 mM	
Chloride	<mark>4</mark> mM	110 mM	

Analysis of various genomes revealed that about 10% of **all** proteins function in **transport** (in E.coli – 427 transporters)

In eucaryotic cells, 2/3 of cellular energy at rest is used to transport ions (H⁺, K⁺, Na⁺, Ca⁺⁺)

About 200 families of transporters are recognized The largest family: ABCtransporters

Transport Processes in an Idealized Eukaryotic Cell



The membrane potential control



The effect of changes in external chloride ion concentration on the membrane potential of an isolated frog muscle fibre (*Hodgkin & Horowicz, 1959*)

One electrode monitors membrane potential (V_m) and the other passes enough current (I_m) through the membrane to clamp V_m to a predetermined command voltage $(V_{command})$.



Four major contributors to the work required to transfer ion from the aqueous environment into the membrane:



Born Energy

$$W_{total} = W_{Born} + W_{image} + W_{dipole} + W_{neutral}$$

$$G = u_{(self)} = W_{Born} = \frac{q^2}{8\pi\varepsilon_0 \varepsilon a}$$

Born (self) energy of an ion in the medium with dielectric coefficient ε (i.e. the work required to charge the ion from 0)

If the ion is transferred between media with different dielectric constants:

$$\Delta U = \Delta W_{Born} = \frac{q^2}{4\pi\varepsilon_0} * \frac{1}{2a} \left(\frac{1}{\varepsilon_2} - \frac{1}{\varepsilon_1}\right) = \frac{cz^2}{2a} \left(\frac{1}{\varepsilon_2} - \frac{1}{\varepsilon_1}\right)$$

 $c = e^2/4\pi\epsilon_0 = 14.4 \text{ eV*}\text{\AA}$

For $\varepsilon_1 = 80$ (water) and $\varepsilon_2 = 2$ (membrane), the Born energy is very large for most ions, i.e., 30-60 kcal/mol for a = 4-2 Å.

Image Forces and Image Charges:

$$W_{total} = W_{Born} + W_{image} + W_{dipole} + W_{neutral}$$

When a charge approaches a dielectric discontinuity:

$$q_{image} = -\left(\frac{\varepsilon_2 - \varepsilon_1}{\varepsilon_2 + \varepsilon_1}\right)Q = tQ$$

$$Force = \frac{tQ^2}{4\pi\varepsilon_0\varepsilon_1(2r)^2}$$

Infinite plane conductor

$$\mathbf{\epsilon}_2 = \infty$$
 $\mathbf{\epsilon}_1$

Image Forces and Image Charges:



Image Forces and Image Charges:







Crossing the Barrier - Membrane Transport Mechanisms

- 1. Diffusive carriers ionophorous antibiotics, *but not proteins*
- 2. Transporters/permeases, etc:
 - 1. Uniporters liver cell glucose transport
 - 2. Symporters epithelial glucose/Na⁺ transport
 - 3. Antiporters red blood cell HCO₃⁻/Cl⁻ transport
- 3. Channels:
 - 1. Unregulated porins; gramicidin A (a channel-type ionophore for monovalent cations)
 - Voltage regulated, e.g., Na⁺ channel Ligand-gated, e.g., nicotinic acetylcholine receptor
- 4. Pumps chemically and conformationally driven

Secondary active transport

Primary active

transport

Movement Across Membranes



Active transport



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Phosphorilation changes protein shape and affinity for solute



Primery active transport

(utilizes energy of ATP hydrolysis)



Active transporters

Classified according to their protein sequence homology and structures.

- *P-type*: Na⁺-K⁺-ATPase, Ca²⁺ and H⁺ pump, P means they have *p*hosphorylation and they all sensitive to vanadate inhibition.
- *V-type*: inner membrane ATPase to regulate H⁺ and adjust proton gradients, v means <u>v</u>acuole type for acidification of lysosomes, endosomes, golgi, and secretory vesicles.
- *F-type:* ATP synthase to generate ATP energy from moving the proton across; F means energy coupling *f*actor. There are F_1 and F_0 subcomplexes: F_1 generates ATP, F_0 lets H^+ go through the membrane.
- *ABC transporters:* <u>A</u>TP-<u>b</u>inding <u>c</u>assette protein for active transport of hydrophobic chemicals and Cl⁻.

Active transport by ATPpowered pumps



ATPase-pump classes

Class	Ρ	F	V	ABC
lon	H ⁺ , Na ⁺ , K ⁺ , Ca ²⁺	H⁺	H⁺	various
Location Example	Na⁺/K⁺ pump	Mitochon- drial F ₁ F ₀	Endo- somes	Bacteria
Function	Maintain Na/K gradients	Generate ATP	Acidify endo- somes	Drug resis- tance

ABC Transporter: transport ATPase

- 1. Largest transport ATPase family (> 50 members)
- 2. In procaryotes, the transporter locates in the inner membrane to carry nutrients into the cell
- 3. In eucaryotes: multidrug resistance (MDR) protein, which produce resistance to drug.
- 4. Cyctic fibrosis: a mutation on one ABC transporter (cyctic fibrosis transmembrane regulator [CFTR] protein) that function as a CI⁻ channel in the epithelial



Some examples:

The master pump concept

A Creates transmembrane gradient of a selected ion.

4 Other ions and molecules are transported across the membrane by coupling their movement to the movement of the selected ion.

4 The electrochemical potential energy is stored only across the membrane in which the pump is located.

Ion gradients generally store smaller packets of energy than ATP - coupled transporters (increased efficiency).

Coupling transport to a single master pump serve a control function.



Atributes of a master pump

Low dissipation (leakage current) is the reason that pumps almost exclusively transport the relatively impermeant inorganic cations.

High capacity – the ion gradient involve concentrations that are relatively large compared to the concentrations of the compounds that are to be transported.

High efficiency





Na⁺,K⁺-ATPase

Abundance reflects importance

– Erythrocyte = 20-30 copies – Heart cell or neuron > 100,000 copies



Primary active transport

 $3Na^{+}(in) + 2K^{+}(out) + ATP + H_2O \iff 3Na^{+}(out) + 2K^{+}(in) + ADP + Pi$







Jens Skou Receives 1997 Nobel Prize for Discovery of Na,K-ATPase

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THE INFLUENCE OF SOME CATIONS ON AN ADENOSINE TRIPHOSPHATASE FROM PERIPHERAL NERVES

BIOCHIMICA RT BIOPHYSICA ACTA

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Na⁺,K⁺-ATPase Functions

20% of body heat in mammals is from the basal activity of Na^+, K^+ -ATPase.

 $\square > 30\%$ of metabolic energy in resting mammals is consumed by Na^+, K^+ -ATPase.



Cardiac glycosides bind exclusively to the extracellular surface of Na^+, K^+ -ATPase when it is in the E_2 -P state.

When pump is stopped



After inhibition of the Na–K pump with ouabain, continued passive leakage disrupts equilibrium. To counteract this, water flows into the cell causing it to swell.



A transport system might not be coupled to the master pump Ca²⁺-ATPase



Plasma membrane Ca²⁺-ATPase



Calcium homeostasis

Cytoplasmic Ca^{2+} is regulated by a Na⁺/Ca²⁺ antiporter in plasma membranes and by P-type Ca-ATPases in plasma membranes and endoplasmic reticulum.

Sarcoplasmic Reticulum Ca2+ - ATPase

[also on ER, hence "SERCA" pump]



Secondary Active Transport (Coupled Transport)

Utilizes ion-gradients generated by primary transporters.



Secondary active transport

Nerst equation

Uniport – transport of a single solute driven only by $\Delta \Psi$

$$\log_{10} \frac{[S_I^{+Z}]}{[S_O^{+Z}]} = -Z \frac{\Delta \Psi}{B}$$

 $2.3RT/F = 59 mV = B at 25^{\circ}C$

Uniport



Symport (cotransport) amino acids and sugers

Et the equilibrium

$$\Delta G_{S^{Z^{+}}} = n \Delta \widetilde{\mu}_{H^{+}} + \Delta \widetilde{\mu}_{S^{Z^{+}}} = 0$$

n is the number of moles of H^+ that would have to move down the $\Delta\mu_{J^+}$ gradient to generate the accumulation.

Symport

$$\begin{split} \Delta \widetilde{\mu}_{H^+} &= F \Delta \Psi - 2.3 RT \Delta p H \\ \Delta \widetilde{\mu}_{S^{Z^+}} &= 2.3 RT \log_{10} \frac{[S_I^{+Z}]}{[S_O^{+Z}]} + z F \Delta \Psi \\ \Delta G_{S^{Z^+}} &= \Delta \widetilde{\mu}_{S^{Z^+}} + \Delta \widetilde{\mu}_{H^+} = 2.3 RT \log_{10} \frac{[S_I^{+Z}]}{[S_O^{+Z}]} + z F \Delta \Psi + n (F \Delta \Psi - 2.3 RT \Delta p H) = 0 \\ \log_{10} \frac{[S_I^{+Z}]}{[S_O^{+Z}]} &= n \Delta p H - (n+z) \frac{\Delta \Psi}{B} \end{split}$$

 $2.3RT/F = 59 mV = B at 25^{\circ}C$

Antiport (counter-transport) restricted to ions

$$\Delta \widetilde{\mu}_{S^{+Z}} = 2.3RT \log_{10} \frac{S_0^{+Z}}{S_I^{+Z}} - zF\Delta \Psi$$
$$\Delta \widetilde{\mu}_{H^+} = F\Delta \Psi - 2.3RT\Delta pH$$

Antiport

 \mathbf{S}_2

 S_1

4 Combining $\Delta \mu_{H+}^{\sim}$ and $\Delta \mu_{S+Z}^{\sim}$

$$\log_{10} \frac{S_I^{+Z}}{S_O^{+Z}} = (n-z)\frac{\Delta \Psi}{Z} - n\Delta pH$$

n is the number of moles of H^+ that would have to move againsty the $\Delta \mu_{J^+}^$ gradient to generate the accumulation.

4 If n = z, then the charge movement would be neutral and ΔΨ has no effect.

$$\log_{10} \frac{S_I^{+Z}}{S_O^{+Z}} = -n\Delta pH$$

The consequence of the transfer of charged malecules

Electroneutral

Electrogenic



A potential difference across a biological membrane: $\sim 70 \text{ mV}$

The voltage gradient is $\sim 20,000,000 V/m$.

Integration of a transport systems !!!



Secondary active transport example

• Works if
$$|n_{ions}\Delta G_{driving ion}| > |n_{transportee}\Delta G_{transportee}|$$

- Sodium-Glucose cotransporter (1:1)
- Intestinal glucose around 0.5 mM
- Intestinal epithelial intracellular glucose >5 mM
- $\Delta G_{\text{glucose IN}} = +1,418 \text{ cal/mol}$
- $\Delta G_{\text{sodium IN}} = -3,261 \text{ cal/mol}$
- So one sodium CAN drive the import of one glucose from the interior of your intestine!



Na⁺/glucose cotransporter Energetics of transport: Entry of 1 sodium contributes about 2.2-3 kcal/mol For uncharged glucose $\Delta G = RTln([C_2]/[C_1])$ Therefore co-transport with 2 Na⁺ allows to generate about 1000 fold higher concentration of glucose inside the cell

$$\Delta G = \sum_{i} n_{i} \Delta \mu_{i} = \sum_{i} n_{i} (\mu_{i}^{in} - \mu_{i}^{out}) = \sum_{i} n_{i} \left[RT \ln \left(\frac{C_{in}}{C_{out}} \right) + z_{i} F \psi_{m} \right]$$

At equilibrium:
$$\Delta G = RT \ln \left(\frac{[G]_{in}}{[G]_{out}} \right) + RT \ln \left(\frac{[Na^{+}]_{in}}{[Na^{+}]_{out}} \right) + F \psi_{m} = 0$$
$$\frac{[G]_{in}}{[G]_{out}} = \left(\frac{[Na^{+}]_{out}}{[Na^{+}]_{in}} \right) \exp(-F \psi_{m} / RT)$$



E. coli lactose transporter

Acidification of the stomach lumen The role of H⁺/K⁺ ATPase

This is the largest concentration Basolateral Apical membrane membrane gradient (pH = 1.0; Cl⁻channel pH = 7.5) protein Anion antiport across a membrane in protein HCO₃ HCO3-ATP eukaryotic organisms! H⁺/K⁺ ATPase ADP H₂O Carbonic anhydrase K⁺ channel CO₂ + OH protein CO₂

Stomach lumen

Tight junction

Regulation of intracellular pH

- Intracellular pH (pH_i) ~ 7.0-7.2
- Extracellular $pH(pH_e) \sim 7.4$
- Metabolic processes produce acidic byproducts $\Rightarrow \downarrow pH_i$
- Require regulatory mechanisms to maintain pH_i



Na/H exchanger

Because of V_m , pH_{in} would equilibrate at ~ 6.4 without a mechanism to move H^+ out.

 \Box Exchanges H⁺ for Na⁺ *electroneutrally*, unaffected by membrane voltage.

Direction of exchange is determined by concentration ratios of the ions in and out.

At equilibrium,

 $[Na^+]_{out}/[Na^+]_{in} = [H^+]_{out}/[H^+]_{in}$

 pH_{in} would be ~ 8.4, but exchanger turns off when pH_{in} rises into the range of 7.0 - 7.4.

 $[Na^+]_{out}$ is ~10⁶ times greater than $[H^+]_{in}$, one-for-one exchange of H ⁺ for Na⁺ can substantially change $[H^+]_{in}$ with almost no change in Na⁺ concentrations, so $\Delta[Na^+]$ driving force remains strong as $\Delta[H^+]$ diminishes.



Comparison of transport mechanisms

Transport rate [s⁻¹]

Channels/Pores - Often very high rate (when open) Sodium Channel 10^{7} 10^{8} Gramicidin A (H⁺) Acetylcholine receptor channel 10^{7} Passive Permeases (Carriers, Transporters) *valinomycin* (carrier) 10^{4} H⁺ - Lactose permease (*E. coli*) - symport 30 Glucose transporter (erythrocytes) - uniport 300 Band 3 anion transporter (erythrocytes) - Cl⁻/HCO₃ - antiport 10^{5} **Primary Active Transporters** Bacteriorhodopsin (H⁺), Halorhodopsin (Cl⁻) 100 Na⁺/K⁺-ATPase (P-type) 450 H⁺-ATPase (F-type) 500 Simple diffusion (nonpolar compounds only Cytochrome c oxidase (H⁺) 1000 down concentration gradient



Bulk transport

Endocytosis



Exocytosis



Cystic Fibrosis and Membrane Transport

Cystic Fibrosis

CF causes the body to produce an abnormally thick, sticky mucus on epithelial surfaces.



It is one of the most common lethal inherited disorders among caucasians.

One in 28 Caucasians - is an unknowing, symptom-less heterozygous carrier of the defective gene

Symptoms and complications

- Decreased mucociliary clearance of sputum leads to chronic endobronchial bacterial colonization, and...
 - Production of large amounts of sputum
 - Wheezing
 - Dyspnea
 - Limited exercise tolerance
 - Death



- Pancreatic insufficiency in 85% of patients, leading to malabsorption of fat and malnutrition.
- Also diabetes mellitus, bowel obstructions, arthritis, and infertility.

Cystic Fibrosis Transconductance Regulator (CFTR)

- A member of the ABC superfamily of transport proteins
- However, it does not appear to act as an *active* transporter
- A chloride channel facilitated diffusion
- Activated by phosphorylation
- Permits chloride movement to the epithelial surface.
- This results in osmotic flux of water to the apical surface, diluting mucus.
- In about 70% of CR cases, a mutated form of the CFTR is reaches the ER, but is then degraded.





Current treatments

- Treatment for Lung Problems
 - Antibiotics
 - Chest physical therapy (like percussion)
 - Exercise
 - Other medications
 - Anti-inflammatory medications
 - Bronchodilators,
 - Mucus-thinning drugs
 - Oxygen Therapy
- Lung Transplantation
- Management of Digestive Problems
 - Oral pancreatic enzymes
 - Fat-soluble vitamins A, D, E, and K
 - Feeding tube
 - Enemas and mucus-thinning medications to treat intestinal blockages



- (A) A one-dimensional sensor, such as talin, can unfold and elongate with tension. Such a conformational change could expose cryptic binding sites within the protein.
- (B) A membrane channel that opens in response to membrane tension is an example of a two dimensional sensor that increases its in-plane area (A). The panel shows the predicted tilting motion of pairs of transmembrane helices of the bacterial mechanosensitive channel MscL, which are associated with a ,20 nm² change of in-plane area expansion.
- (C) A hypothetical elastic structure that decreases its volume under osmotic pressure is an example of a three-dimensional mechanosensor.

Transport System Integration



Examples of Types of Na+-coupled Transporters

Transport System Integration



Examples of Types of Na+-coupled Transporters

- When the Na⁺,K⁺-ATPase is inhibited
 - [K⁺] decreases in cytosol.
 - [Na⁺] increases in cytosol.
- At the Na⁺, Ca²⁺ antiporter,
 - Affinity of transporter for Na⁺ at cytosolic binding site is close to intracellular [Na⁺].
 - If intracellular [Na⁺] increases,
 Na⁺ will compete more effectively with Ca²⁺ at transporter.
 - Increased Na⁺ competition results in less Ca²⁺ efflux.
 - Less Ca²⁺ efflux results in increased intracellular free Ca²⁺.